

Fig. 1. The molecular structure of $\mathrm{RhH}\left(\mathrm{PPh}_{3}\right)_{2}\left(\mathrm{C}_{2} \mathrm{~B}_{9} \mathrm{H}_{11}\right)$. All hydrogen atcms except the hydride are omitted for clarity. A atoms except the phenyl carbon atoms are depicted as $50 \%$ probability ellipsoids.

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# An Efficient Laser Material, Lithium Neodymium Phosphate LiNdP $\mathbf{4 O}_{\mathbf{1 2}}$ 

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Abstract. Monoclinic, $I 2 / c\left(C_{2 h}^{6}\right), a=9 \cdot 844$ (2), $b=$ 7.008 (3), $c=13.25$ (2) $\AA, \beta=90 \cdot 1$ (2) ${ }^{\circ}, Z=4, D_{c}=3 \cdot 39$, $D_{o}=3.38 \mathrm{~g} \mathrm{~cm}^{-3}, \mu(\mathrm{Mo} K \alpha)=62.0 \mathrm{~cm}^{-1}$. Structural framework is helical chains of $\left(\mathrm{PO}_{3}\right)_{\infty}$ along the $b$ axis. Both $\mathrm{Nd}^{3+}$ and $\mathrm{Li}^{+}$ions alternate on twofold axes in the middle of four such chains. $\mathrm{NdO}_{8}$ dodecahedra and considerably distorted $\mathrm{LiO}_{4}$ tetrahedra form linear chains sharing their edges. The refinement converged to $R=0.035$ for 1095 independent observed reflexions.

Introduction. Recently a phosphate laser material with high Nd concentration, $\mathrm{LiNdP}_{4} \mathrm{O}_{12}$, was produced in our laboratory and is reported to have a high laser performance (Yamada, Otsuka \& Nakano, 1974), comparable to or better than that of $\mathrm{NdP}_{5} \mathrm{O}_{14}$.

Specimens were selected from the crystals grown from the melt of $\mathrm{Li}_{2} \mathrm{O}-\mathrm{Nd}_{2} \mathrm{O}_{3}-\mathrm{P}_{2} \mathrm{O}_{5}$ by the Kyropolous technique (Yamada et al., 1974). Precession and Weissenberg photographs exhibited $2 / m$ Laue symme-
try with the following systematic absences: $h k l$ when $h+k+l=2 n+1,0 k l$ when $k+l=2 n+1, h 0 l$ when $h=2 n+1, l=2 n+1, h k 0$ when $h+k=2 n+1$.*

A prismatic crystal of dimensions $0.23 \times 0.35 \times 0.63$ mm was mounted so that its $b$ axis was along the $\varphi$ axis of the Rigaku Denki automatic four-circle X-ray diffractometer. Reflexions within $(\sin \theta / \lambda)=0.60 \AA^{-1}$ were measured using $\omega-2 \theta$ scan technique with a Ge monochromator. The intensities were corrected for Lorentzpolarization, absorption and extinction effects.

The locations of the heavier atoms, $\mathrm{Nd}^{3+}$ and P , were determined by the three-dimensional Patterson method. Structure factors based on the Patterson coordinates gave the conventional $R$ value of $0 \cdot 231$. Successive Fourier synthesis clearly revealed the O atoms' positions indicating tetrahedral coordination around

[^0]each P atom. Then atomic positional and thermal parameters were refined by a full-matrix least-squares method (Busing, Martin \& Levy, 1962) to give $R=$ 0.067 . The location of the $\mathrm{Li}^{+}$ion was selected from among several possible sites on the basis of symmetry and bonding considerations. All parameters including those for the $\mathrm{Li}^{+}$ion were refined by two further cycles of least-squares methods and a final $R$ value of 0.035 was obtained.
The final atomic positional and thermal parameters are listed in Table 1.*

Discussion. Bond distances and angles calculated from the final parameters are given in Table 2. Views of the structure projected along each axis are shown in Figs. 1,2 and 3.

* A list of structure factors has been deposited with the British Library Lending Division as Supplementary Publication No. SUP 31343 ( 7 pp .). Copies may be obtained through The Executive Secretary, International Union of Crystallography, 13 White Friars, Chester CH1 1NZ, England.

Table 1. Positional and thermal parameters obtained in the final least-squares refinement Estimated standard deviations are given in parentheses. Anisotropic thermal factors ( $\times 10^{5}$ ) are given by the expression: $T=\exp \left[-\left(h^{2} \beta_{11}+k^{2} \beta_{22}+l^{2} \beta_{33}+2 h k \beta_{12}+2 k l \beta_{23}+2 h l \beta_{13}\right)\right]$.

|  | $x$ | $y$ | $z$ | $\beta_{11}$ or $B\left(\AA^{2}\right)$ | $\beta_{22}$ | $\beta_{33}$ | $\beta_{12}$ | $\beta_{13}$ | $\beta_{23}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Nd | ${ }^{\frac{1}{2}}$ | $0 \cdot 5501$ (1) | $\frac{1}{4}$ | 231 (6) | 471 (12) | 86 (3) | 0 | 8 (3) | 0 |
| $\mathrm{P}(1)$ | $0 \cdot 2247$ (2) | $0 \cdot 3070$ (2) | $0 \cdot 3889$ (1) | 261 (14) | 614 (30) | 91 (8) | 8 (15) | 20 (8) | 15 (11) |
| P (2) | $0 \cdot 3021$ (2) | $0 \cdot 9081$ (3) | $0 \cdot 3990$ (1) | 287 (15) | 594 (28) | 91 (8) | -6 (16) | 7 (8) | 3 (12) |
| $\mathrm{O}(1)$ | $0 \cdot 1193$ (5) | $0 \cdot 2551$ (6) | $0 \cdot 3153$ (3) | 328 (39) | 630 (79) | 105 (20) | 121 (41) | 31 (22) | 26 (33) |
| O(2) | $0 \cdot 3155$ (5) | $0 \cdot 4689$ (6) | $0 \cdot 3651$ (4) | 448 (50) | 548 (92) | 188 (27) | - 172 (46) | 49 (30) | 42 (34) |
| O(3) | $0 \cdot 1554$ (4) | $0 \cdot 8642$ (6) | $0 \cdot 3806$ (3) | 334 (41) | 627 (86) | 171 (23) | 26 (47) | -91 (25) | 20 (35) |
| $\mathrm{O}(4)$ | $0 \cdot 4072$ (4) | $0 \cdot 8490$ (6) | $0 \cdot 3238$ (3) | 370 (42) | 634 (84) | 176 (23) | 17 (44) | 104 (25) | 15 (36) |
| O(5) | $0 \cdot 1488$ (4) | $0 \cdot 3364$ (7) | $0 \cdot 4937$ (3) | 333 (40) | 985 (90) | 64 (20) | 23 (48) | -15 (23) | -36 (35) |
| O(6) | $0 \cdot 3231$ (4) | 0.1321 (6) | $0 \cdot 4095$ (3) | 329 (4) | 163 (5) | 208 (3) | 85 (41) | 1 (80) | -3 (23) |
| Li | $\frac{1}{2}$ | 0.0536 (18) |  | [0.98 (9)] |  |  |  |  |  |

Table 2. Bond distances and angles in $\mathrm{LiNdP}_{4} \mathrm{O}_{12}$ with standard deviations in parentheses
Dodecahedron around Nd

| Dodecahedron around | Nd-O(1) | $2 \times 2.571$ (4) $\AA$ A | $\mathrm{O}(1)-\mathrm{O}(1)^{\prime}$ | 2.854 (7) $\AA$ A |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  | $\mathrm{Nd}-\mathrm{O}(2)$ | $2 \times 2.421$ (5) | $\mathrm{O}(1)-\mathrm{O}(2)$ | 2.934 (6) |  |
|  | Nd-O(3) | $2 \times 2.404$ (4) | $\mathrm{O}(1)-\mathrm{O}(3)$ | 2.904 (6) |  |
|  | Nd-O(4) | $2 \times 2.480$ (4) | $\mathrm{O}(2)-\mathrm{O}(4)$ | $2 \cdot 863$ (6) |  |
|  | $\mathrm{Nd}-\mathrm{Nd}$ | 6.474 (1) | $\mathrm{O}(3)-\mathrm{O}(4)$ | 2.971 (6) |  |
|  |  | $5 \cdot 644$ (1) | $\mathrm{O}(3)-\mathrm{O}(4)$ | $3 \cdot 162$ (6) |  |
|  |  | $6 \cdot 662$ (1) | $\mathrm{O}(4)-\mathrm{O}(4)^{\prime}$ | $2 \cdot 655$ (6) |  |
| Tetrahedron around $\mathbf{P}(1)$ |  |  |  |  |  |
| $\mathrm{P}(1)-\mathrm{O}(1)$ | 1.519 (5) $\AA$ | $\mathrm{O}(1)-\mathrm{O}(2)$ | 2.581 (7) $\AA$ | $\mathrm{O}(1)-\mathrm{P}(1)-\mathrm{O}(2)$ | 119.1 (3) ${ }^{\circ}$ |
| $\mathrm{P}(1)-\mathrm{O}(2)$ | $1 \cdot 475$ (5) | $\mathrm{O}(1)-\mathrm{O}(5)$ | $2 \cdot 461$ (6) | $\mathrm{O}(1)-\mathrm{P}(1)-\mathrm{O}(5)$ | $105 \cdot 1$ (3) |
| $\mathrm{P}(1)-\mathrm{O}(5)$ | 1.580 (4) | $\mathrm{O}(1)-\mathrm{O}(6)$ | 2.574 (6) | $\mathrm{O}(1)-\mathrm{P}(1)-\mathrm{O}(6)$ | 111.8 (2) |
| $\mathrm{P}(1)-\mathrm{O}(6)$ | 1.589 (4) | $\mathrm{O}(2)-\mathrm{O}(5)$ | 2.574 (6) | $\mathrm{O}(2)-\mathrm{P}(1)-\mathrm{O}(5)$ | $111 \cdot 3$ (3) |
|  |  | $\mathrm{O}(2)-\mathrm{O}(6)$ | 2.434 (6) | $\mathrm{O}(2)-\mathrm{P}(1)-\mathrm{O}(6)$ | $105 \cdot 1$ (3) |
|  |  | $\mathrm{O}(5)-\mathrm{O}(6)$ | $2 \cdot 485$ (6) | $\mathrm{O}(5)-\mathrm{P}(1)-\mathrm{O}(6)$ | $103 \cdot 3$ (2) |
| Tetrahedron around $\mathrm{P}(2)$ l |  |  |  |  |  |
| $\mathrm{P}(2)-\mathrm{O}(3)$ | 1.500 (4) $\AA$ | $\mathrm{O}(3)-\mathrm{O}(4)$ | 2.581 (6) $\AA$ | $\mathrm{O}(3)-\mathrm{P}(2)-\mathrm{O}(4)$ | 119.6 (2) ${ }^{\circ}$ |
| $\mathrm{P}(2)-\mathrm{O}(4)$ | $1 \cdot 484$ (4) | $\mathrm{O}(3)-\mathrm{O}(5)$ | 2.575 (6) | $\mathrm{O}(3)-\mathrm{P}(2)-\mathrm{O}(5)$ | $112 \cdot 6$ (2) |
| $\mathrm{P}(2)-\mathrm{O}(5)$ | 1.590 (4) | $\mathrm{O}(3)-\mathrm{O}(6)$ | 2.533 (6) | $\mathrm{O}(3)-\mathrm{P}(2)-\mathrm{O}(6)$ | $110 \cdot 1$ (3) |
| $\mathrm{P}(2)-\mathrm{O}(6)$ | 1.590 (5) | $\mathrm{O}(4)-\mathrm{O}(5)$ | 2.473 (6) | $\mathrm{O}(4)-\mathrm{P}(2)-\mathrm{O}(5)$ | $107 \cdot 2$ (3) |
|  |  | $\mathrm{O}(4)-\mathrm{O}(6)$ | $2 \cdot 425$ (6) | $\mathrm{O}(4)-\mathrm{P}(2)-\mathrm{O}(6)$ | $104 \cdot 1$ (3) |
|  |  | $\mathrm{O}(5)-\mathrm{O}(6)$ | $2 \cdot 455$ (6) | $\mathrm{O}(5)-\mathrm{P}(2)-\mathrm{O}(6)$ | 101•1 (2) |
| Tetrahedron around Li |  |  |  |  |  |
| $\mathrm{Li}-\mathrm{O}(1)$ | $2 \times 1.958$ (12) $\AA$ | $\mathrm{O}(1)-\mathrm{O}(4)$ | $2 \times 3.441$ (6) $\AA$ | $\mathrm{O}(1)-\mathrm{Li}-\mathrm{O}(4)$ | $2 \times 123.2(2)^{\circ}$ |
| $\mathrm{Li}-\mathrm{O}(4)$ | $2 \times 1.954$ (9) | $\mathrm{O}(1)-\mathrm{O}(4)^{\prime}$ | $2 \times 3.339$ (6) | $\mathrm{O}(1)-\mathrm{Li}-\mathrm{O}(4)^{\prime}$ | $2 \times 93.6$ (6) |
|  |  | $\mathrm{O}(1)-\mathrm{O}(1)^{\prime}$ | 2.854 (6) | $\mathrm{O}(1)-\mathrm{Li}-\mathrm{O}(1)^{\prime}$ | 117.2 (2) |
|  |  | $\mathrm{O}(4)-\mathrm{O}(4)^{\prime}$ | $2 \cdot 655$ (6) | $\mathrm{O}(4)-\mathrm{Li}-\mathrm{O}(4)^{\prime}$ | 85.6 (5) |



Fig. 1. [010] projection of the $\mathrm{LiNd}_{4} \mathrm{O}_{12}$ structure.


Fig. 2. [100] projection of the $\mathrm{LiNdP}_{4} \mathrm{O}_{12}$ structure.


Fig. 3. Schematic view of the $-\mathrm{NdO}_{8}-\mathrm{LiO}_{4}$ - chain in the [001] direction.

Each $\mathrm{NdO}_{8}$ dodecahedron on the twofold axes also has an approximate $\overline{4}$ symmetry along the $b$ axis. Such a configuration can be seen also in the crystal structure of $\mathrm{NdNa}_{5}\left(\mathrm{WO}_{4}\right)_{4}$ (Hong \& Dwight, 1974). The polyhedra share all their oxygen atoms with the corners and edges of neighbouring $\mathrm{PO}_{4}$ and $\mathrm{LiO}_{4}$ tetrahedra respectively. It is to be noted that the adjacent $\mathrm{NdO}_{8}$ polyhedra do not share any oxygen atoms among them. The shortest $\mathrm{Nd}-\mathrm{Nd}$ distance $5.644 \AA$ is an intermediate value of those in $\mathrm{NdNa}_{5}\left(\mathrm{WO}_{4}\right)_{4}(6.450 \AA)$ and $\mathrm{NdP}_{5} \mathrm{O}_{14}(5 \cdot 194 \AA)$ (Albrand, Attig, Fenner, Jeser \& Mootz, 1974).
$\mathrm{LiO}_{4}$ tetrahedra have a considerably distorted shape with a somewhat shorter average $\mathrm{Li}-\mathrm{O}$ distance ( $1.956 \AA$ ) than that quoted in the literature ( $1.98 \AA$ ), International Tables for X-ray Crystallography (1962).

The helical arrangement of the corner-shared $\mathrm{PO}_{4}$ tetrahedra chains can be clearly shown on [100] and [001] projection (Figs. 2 and 3). In comparison, helical chains in the $\mathrm{NdP}_{3} \mathrm{O}_{9}$ structure involve two more $\mathrm{PO}_{4}$ groups in each chain unit and in the structure of $\mathrm{NdP}_{5} \mathrm{O}_{14}$ there is cross-linking of $\left(\mathrm{PO}_{3}\right)_{\infty}$ ribbons (Hong, 1974).

The helical $\left(\mathrm{PO}_{3}\right)_{\infty}$ chains in the structure and significant difference in $\mathrm{Nd}-\mathrm{Nd}$ separation along each axis ( $5.644,7.008,6.621 \AA$ ) may be closely related to the observed strong anisotropy in laser characteristics (Otsuka, Yamada, Saruwatari \& Kimura, 1975).

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[^0]:    * The symmetry of the crystal was erroneously reported as orthorhombic (Yamada et al., 1974). The relations between pseudo-orthorhombic axes and monoclinic axes are as follows. $a_{\text {pseudo orth. }}\left\|[100]_{\text {monocl. }} ; b_{\text {pseudo orth. }}\right\| c_{\text {monoct. }}$; $c_{\text {pseudo orth. }} \| b_{\text {monocli. }}$.

